

Unlocking ultra-short time-scale many-body entanglement generation through atom-pair coupling to cavity photons

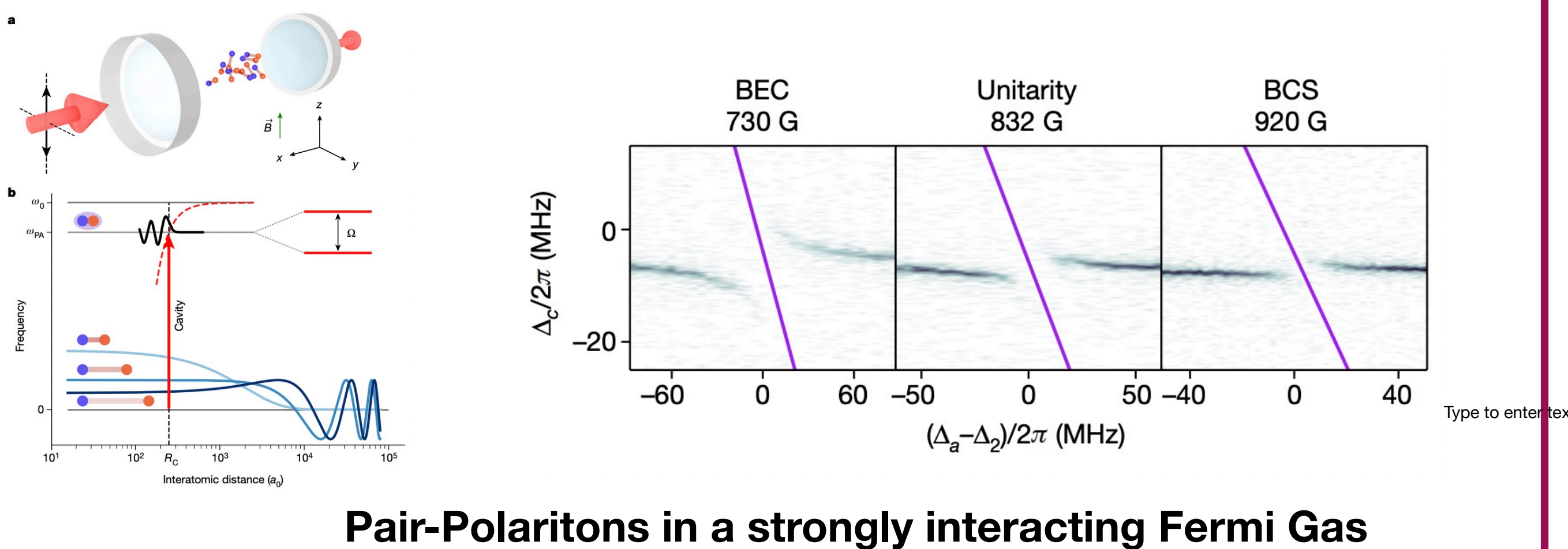
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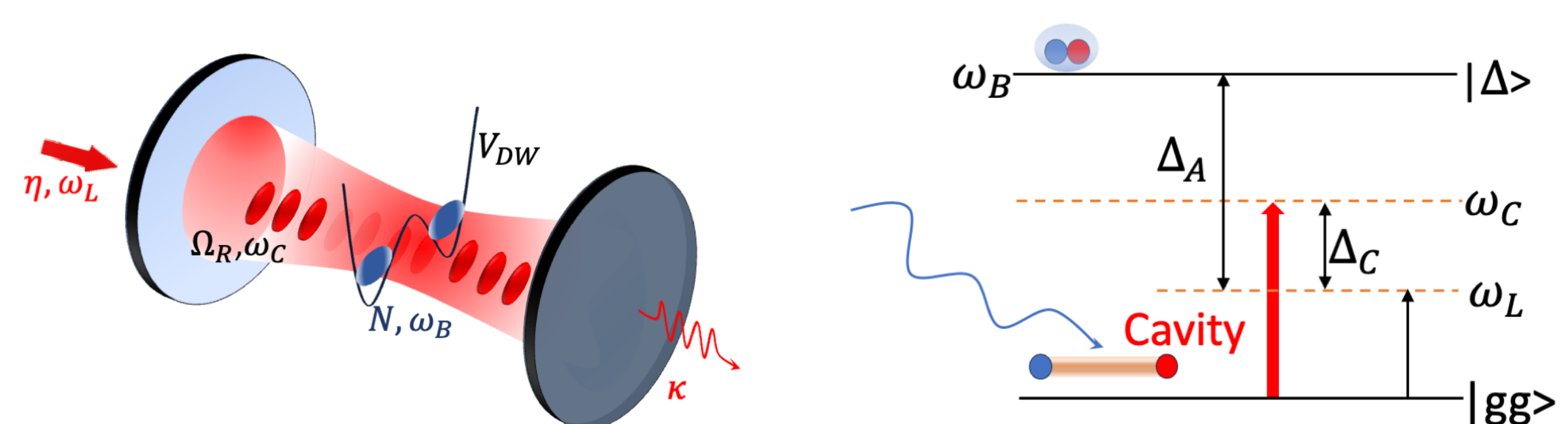
1. INTRODUCTION

- Hybrid light-matter systems: cavity photons + ultracold atomic gas.
- Photon-induced tuneable-range interaction potentials: novel states of matter.
- Atom-photon interactions lead to non-classical states of matter or light.
- Promising way for tuning interaction between atoms via photon exchange in cavity.
- Recently the formation of pair-polaritons was experimentally demonstrated [1].



2. NOVEL APPROACH

- Atom-pair interaction with a single photon.
- Laser pumping: Cavity laser, frequency ω_L and amplitude η through one of its mirrors.
- Atomic states: Electronic ground and optically accessible molecular state ($E_\Delta = \hbar\omega_b$).
- Atomic confinement: Confined by a double-well potential, $V_{DW}(x)$, along x direction.
- Confinement is harmonic, frequency ω_H in the y-z plane.



3a. HAMILTONIAN & TWO MODE APPROXIMATION

The Hamiltonian for hybrid light-matter system is:

$$\hat{H} = \hat{H}_{atomic} + \hat{H}_{molecule} + \hat{H}_{photon} + \hat{H}_{atom-light}$$

$$\hat{H}_{atomic} = \int d^3r \Psi_g^\dagger(r) \left[\frac{\nabla^2}{2m} + V(r) \right] \Psi_g(r) + \frac{1}{2} \int d^3r g \Psi_g^\dagger(r) \Psi_g^\dagger(r) \Psi_g(r) \Psi_g(r)$$

$$\hat{H}_{molecule} = \int d^3r \Psi_\Delta^\dagger \left[\frac{-\nabla^2}{2M} + V(r) - \Delta_A \right] \Psi_\Delta$$

$$\hat{H}_{photon} = -\Delta_C a^\dagger a + \eta (a^\dagger + a)$$

$$\hat{H}_{atom-light} = -i\Omega_R \int d^3r f(r) \left[a \Psi_\Delta^\dagger(r) \Psi_g^2(r) - a^\dagger (\Psi_g^2(r))^\dagger \Psi_\Delta(r) \right]$$

For large atom detuning, we can adiabatically eliminate the molecular state.

Using two mode approximation: $\hat{H}_{eff} \approx \hat{H}_L + \hat{H}_J + \hat{H}_{JL}$

$$\hat{H}_{eff} = -\tilde{\Delta}_C a^\dagger a + \eta (a^\dagger + a) - 2J\hat{J}_x + U\hat{J}_z^2 + 2W_0 a^\dagger a \hat{J}_z^2$$

Atom-atom interaction depends on **quantum state** of cavity photons

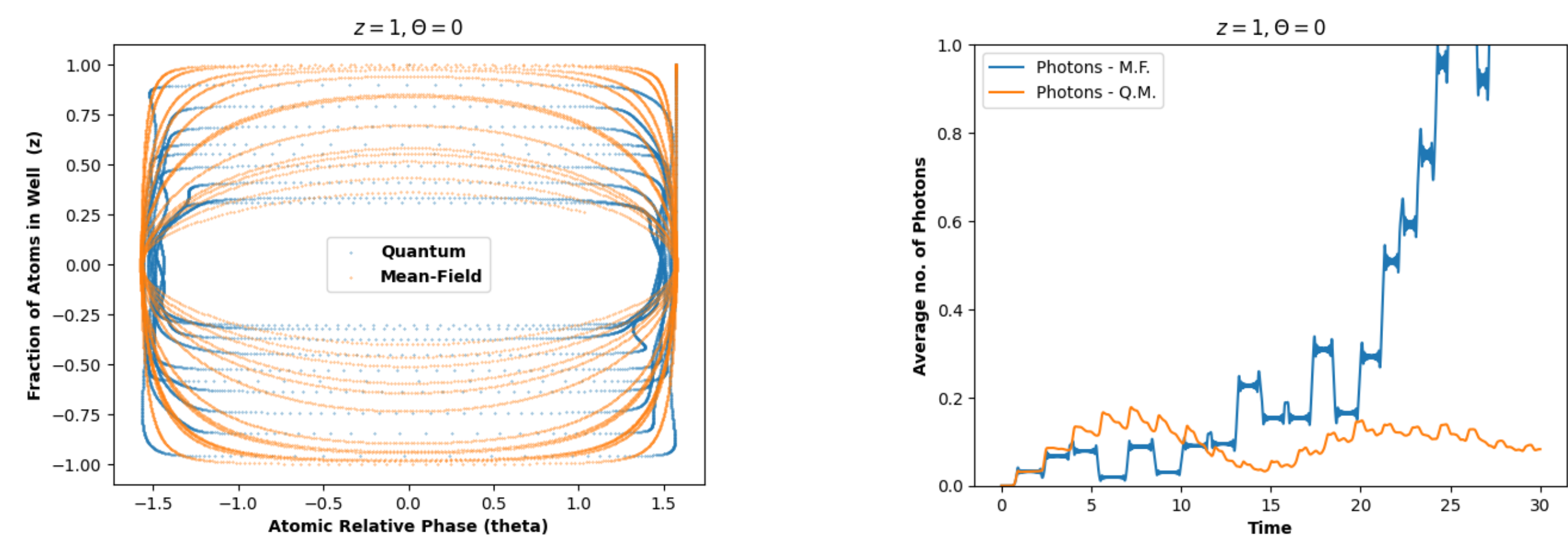
3b. SYMBOLS USED

- ϵ = Single-well energy
- g = Atom-Atom interaction
- J = Tunneling Energy
- U = On-site Interaction strength
- W_0 = Pair-light Interaction
- Δ_A, Δ_C = detuning from: molecular state, cavity photon
- Ω_R = Single mode Rabi frequency

4. MEAN-FIELD vs EXACT DIAGONALIZATION

We can approximate the system in the full coherent state:

$$|FCS\rangle = |\beta_1\rangle_A \otimes |\beta_2\rangle_A \otimes |\alpha\rangle_L$$



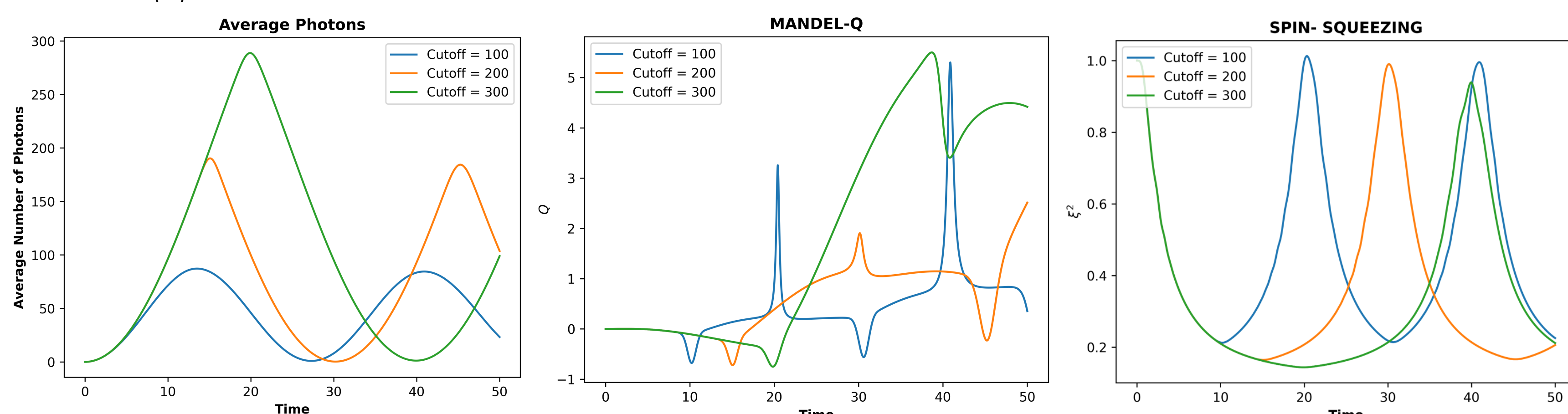
5. QUANTUM CORRELATIONS

1. Atoms: Spin-squeezing

$$\xi^2 = N \frac{\Delta J_z^2}{\langle \hat{J}_x \rangle^2 + \langle \hat{J}_y \rangle^2}, \quad N = \text{total number of atoms. } \xi^2 < 1 \rightarrow \text{entanglement between the atoms}$$

2. Photons : Mandel-Q parameter

$$Q = \frac{\langle (\Delta \hat{n})^2 \rangle - \langle \hat{n} \rangle^2}{\langle \hat{n} \rangle} \quad \hat{n} = \text{number operator. } -1 \leq Q < 0 \rightarrow \text{non-classical light}$$



Non-classical light and entanglement between atoms

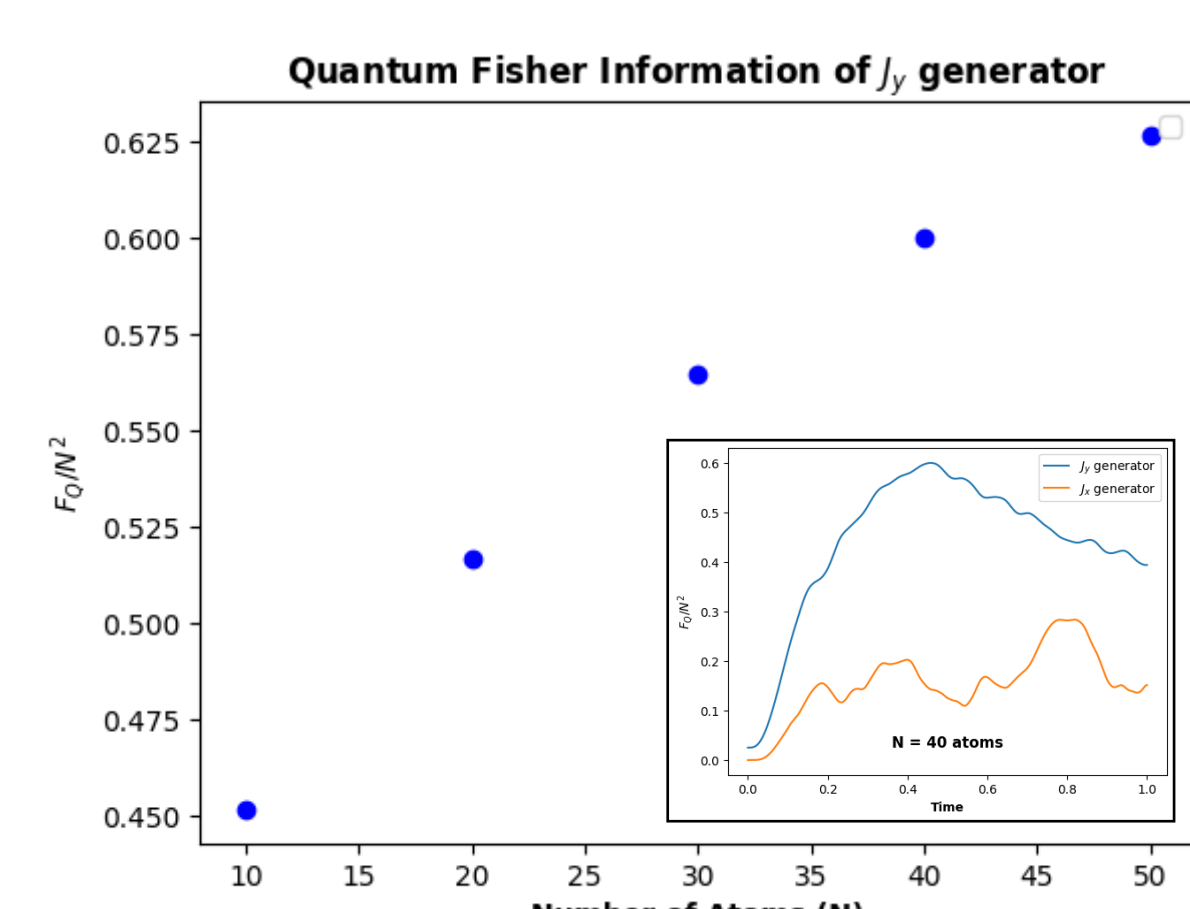
3. Quantum Fisher information

$$F_q = 2 \sum_{i,j} \frac{(\lambda_i - \lambda_j)^2}{\lambda_i + \lambda_j} |\langle \psi_i | \hat{h} | \psi_j \rangle|^2$$

\hat{h} is the interferometric generator.

λ 's and $|\psi\rangle$'s comes from the spectral decomposition of the density matrix

$$\hat{\rho} = \sum_i \lambda_i |\Psi_i\rangle \langle \Psi_i|$$



6. CONCLUSIONS

- Photon-atom-pair interaction → effective atom-atom interaction.
- Dependence on quantum state of cavity photons.
- Non-classical correlations of photons.
- Strong entanglement between atoms.
- Controlled by: detuning, pump, initial photonic state.

7. ACKNOWLEDGEMENT

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8. REFERENCES

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